

1. Nuclei of  ${}^{218}_{84}\text{Po}$  decay by the emission of an  $\alpha$  particle to form a stable isotope of an element X. You may assume that no  $\gamma$  emission accompanies the decay.

(a) (i) State the proton number and the nucleon number of X.

proton number .....

nucleon number .....

(ii) Identify the element X.

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(2)

(b) Each decaying nucleus of Po releases  $8.6 \times 10^{-13}$  J of energy.

(i) State the form in which this energy *initially* appears.

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(ii) Using **only** the information provided in the question, calculate the difference in mass between the original  ${}^{218}_{84}\text{Po}$  atom and the combined mass of an atom of X and an  $\alpha$  particle.

speed of light in vacuum =  $3.0 \times 10^8$  m s<sup>-1</sup>

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(3)

(Total 5 marks)

2. A space probe contains a small fission reactor, fuelled by plutonium, which is designed to produce an average of 300 W of useful power for 100 years. If the overall efficiency of the reactor is 10%, calculate the minimum mass of plutonium required.

energy released by the fission of one nucleus of  ${}_{94}^{239}\text{Pu} = 3.2 \times 10^{-11} \text{ J}$

the Avogadro constant =  $6.0 \times 10^{23} \text{ mol}^{-1}$

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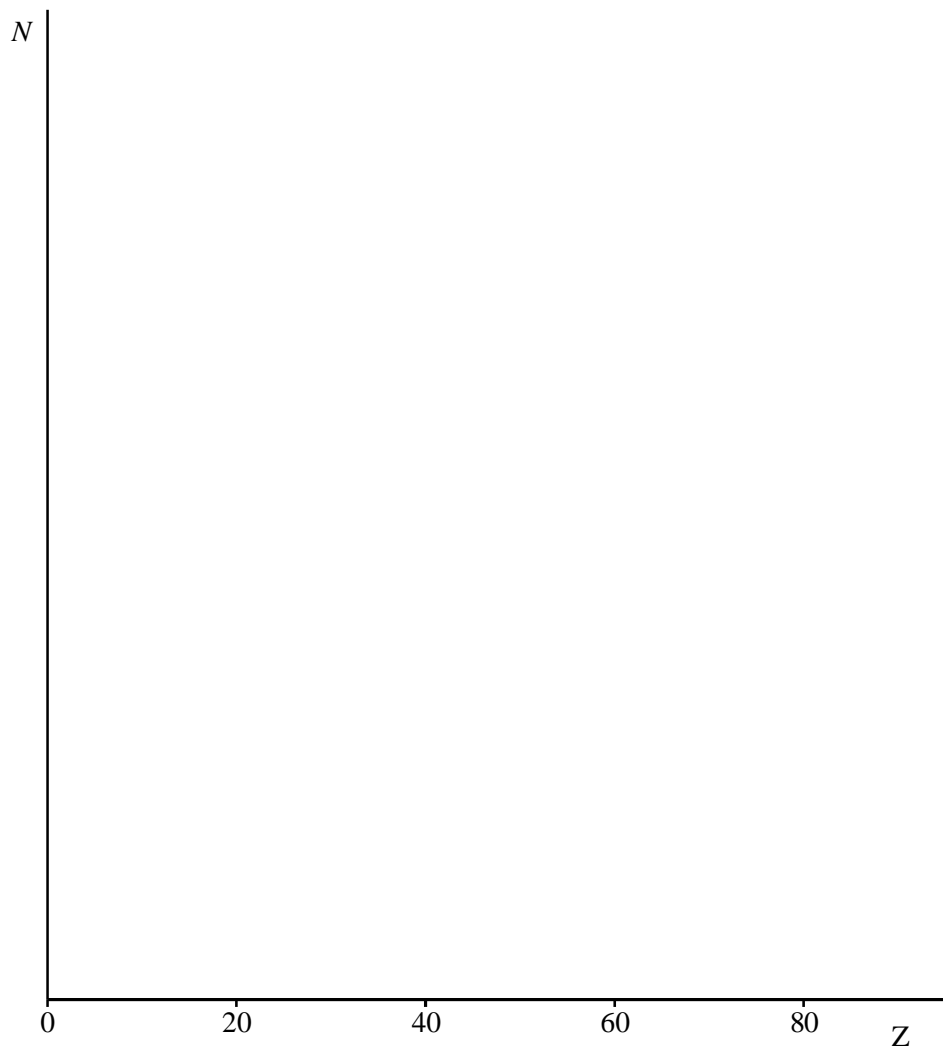
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**(Total 7 marks)**

3. (a) Sketch a graph to show how the number of neutrons,  $N$ , varies with the number of protons,  $Z$ , for stable nuclei over the range  $Z = 0$  to  $Z = 80$ . Draw a scale on the  $N$  axis.



(2)

- (b) On the same graph, enclosing each region by a line, indicate the region in which nuclides are likely to decay, by

- (i)  $\alpha$  emission, labelling the region A,
- (ii)  $\beta^-$  emission, labelling the region B,
- (iii)  $\beta^+$  emission, labelling the region C.

(3)

(c) Complete the table.

mode of decay	change in proton number $Z$	change in neutron number $N$
$\alpha$ emission	-2	
$\beta^-$ emission		
$\beta^+$ emission		
e capture		
p emission		0
n emission	0	

(3)  
(Total 8 marks)

4. (a) State what is meant by the *binding energy* of a nucleus.

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(2)

(b) (i) The iron isotope  ${}_{26}^{56}\text{Fe}$  has a very high binding energy per nucleon. Calculate its value in MeV.

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- (ii) If the isotope  ${}^{56}_{26}\text{Fe}$  were assembled from its constituent particles, what would be the mass change, in kg, during its formation?

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(6)  
(Total 8 marks)

5. (a) An  $\alpha$  particle source of half-life 3420 years has a rate of decay of 450 kBq.  
Calculate

- (i) the decay constant, in  $\text{s}^{-1}$ ,

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- (ii) the number of radioactive atoms in the source.

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(4)

- (b) A narrow beam of  $\alpha$  particles is directed at a thin gold foil target in an evacuated vessel. Only a very small proportion of the  $\alpha$  particles scatter backwards at an angle greater than  $90^\circ$  to the direction from which they came

- (i) Describe what happens to the majority of the  $\alpha$  particles incident on the gold foil.

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- (ii) Several deductions may be made about the structure of gold atoms from the results of  $\alpha$ -particle scattering. Write down **two** of these deductions.

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(3)  
(Total 7 marks)

6. (a) (i) What is meant by the *random nature* of radioactive decay?

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(ii) Explain what is meant by each of the following.

*isotopes* .....

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*radioactive half-life* .....

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*radioactive decay constant* .....

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(6)

(b) The radioactive isotope of iodine  $^{131}\text{I}$  has a half-life of 8.04 days. Calculate

(i) the decay constant of  $^{131}\text{I}$ ,

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- (ii) the number of atoms of  $^{131}\text{I}$  necessary to produce a sample with an activity of  $5.0 \times 10^4$  disintegrations  $\text{s}^{-1}$  (Bq),

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- (iii) the time taken, in hours, for the activity of the same sample of  $^{131}\text{I}$  to fall from  $5.4 \times 10^4$  disintegrations  $\text{s}^{-1}$  to  $5.0 \times 10^4$  disintegrations  $\text{s}^{-1}$ .

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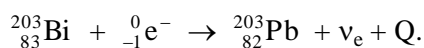
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(6)  
(Total 12 marks)

7. (a) The nuclide  $^{203}_{83}\text{Bi}$  can decay by *electron capture* to become an isotope of lead as shown in the following equation,



- (i) Explain what is meant by electron capture.

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(ii) Give **one** reason why electromagnetic radiation is emitted following this process.

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(iii) Give the equation for another process in which  ${}^{203}_{83}\text{Bi}$  is converted into an isotope of lead.



(5)

(b) The nuclide  ${}^{203}_{83}\text{Bi}$  is also an  $\alpha$  particle emitter. An initial measurement of the  $\alpha$  particle activity of a sample of this isotope gives a corrected count rate of  $1200 \text{ counts s}^{-1}$ . After an interval of 24 hours the corrected rate falls to  $290 \text{ counts s}^{-1}$ . Assume that corrections have been made for the radiation both from daughter products and background radiation.

(i) Show that the decay constant of  ${}^{203}_{83}\text{Bi}$  is about  $1.6 \times 10^{-5} \text{ s}^{-1}$ .

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(ii) Calculate the half-life of this sample.

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- (iii) Calculate the number of  $^{203}_{83}\text{Bi}$  nuclei in the sample when the corrected count rate was  $1200 \text{ counts s}^{-1}$ .

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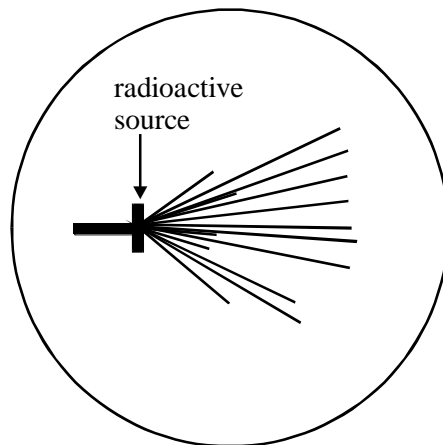
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(5)  
(Total 10 marks)

8. (a) The diagram is copied from a photograph taken of a cloud chamber containing a small radioactive source.



- (i) What type of radiation is emitted from the source?

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- (ii) State and explain what can be deduced about the energy of the particles emitted by the source.

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(4)

- (b) Plutonium  $-239$  is a radioactive isotope that emits  $\alpha$  particles of energy 5.1 MeV and decays to form a radioactive isotope of uranium. This isotope of uranium emits  $\alpha$  particles of energy 4.5 MeV to form an isotope of thorium which is also radioactive.

- (i) Write down an equation to represent the decay of plutonium  $-239$ .

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- (ii) Write down an equation to represent the decay of the uranium isotope.

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- (iii) Which of the two radioactive isotopes, plutonium  $-239$  or the uranium isotope, has the longer half-life? Give a reason for your answer.

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(iv) Explain why thorium is likely to be a  $\beta^-$  emitter.

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(5)  
(Total 9 marks)

9. The radius of a nucleus,  $R$ , is related to its nucleon number,  $A$ , by

$$R = r A^{1/3}, \text{ where } r \text{ is a constant.}$$

The table lists values of nuclear radius for various isotopes.

Element	$R/10^{-15}\text{m}$	$A$	
carbon	2.66	12	
silicon	3.43	28	
iron	4.35	56	
tin	5.49	120	
lead	6.66	208	

- (a) Use the data to plot a straight line graph and use it to estimate the value of  $r$ .

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*(Allow one sheet of graph paper)*

**(8)**

- (b) Assuming that the mass of a nucleon is  $1.67 \times 10^{-27}$  kg, calculate the approximate density of nuclear matter, stating **one** assumption you have made.

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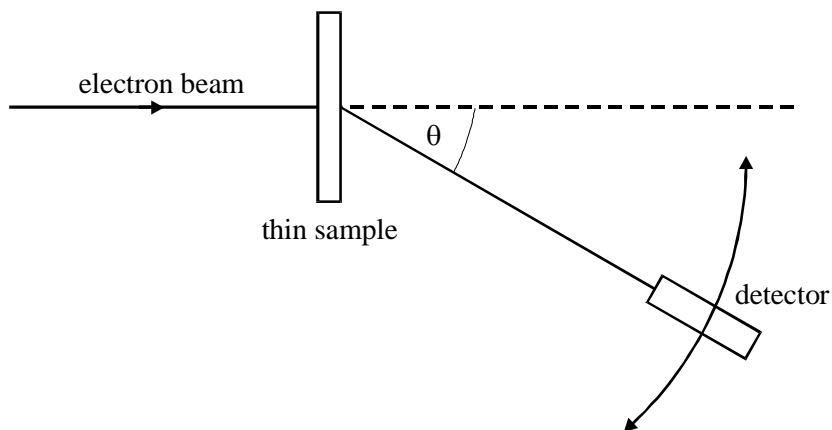
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**(4)**

**(Total 12 marks)**

10. Nuclear radii can be determined by observing the diffraction of high energy electrons, as shown in the diagram.



- (a) On the axes below, sketch a graph of the results expected from such an electron diffraction experiment.



(2)

- (b) State why high energy electrons are used in determining nuclear size.

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(1)

- (c) Electron diffraction experiments have been performed on a range of different nuclei to give information about nuclear density and average separation of particles in the nucleus. Give the main conclusion in each case.

nuclear density .....

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average separation of particles .....

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(2)

- (d) On the axes below, sketch the relationship between the radius of a nucleus and its nucleon number.



(1)

- (e) Given that the radius of the  $^{12}_6\text{C}$  nucleus is  $3.04 \times 10^{-15}\text{m}$ , calculate the radius of the  $^{16}_8\text{O}$  nucleus.

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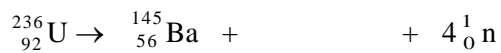
**(3)**  
**(Total 9 marks)**

- 11.** (a) The unstable uranium nucleus  $^{236}_{92}\text{U}$  is produced in a nuclear reactor.

- (i) Complete the equation which shows the formation of  $^{236}_{92}\text{U}$ .



- (ii)  $^{236}_{92}\text{U}$  can decay by nuclear fission in many different ways. Complete the equation which shows one possible decay channel.



**(2)**



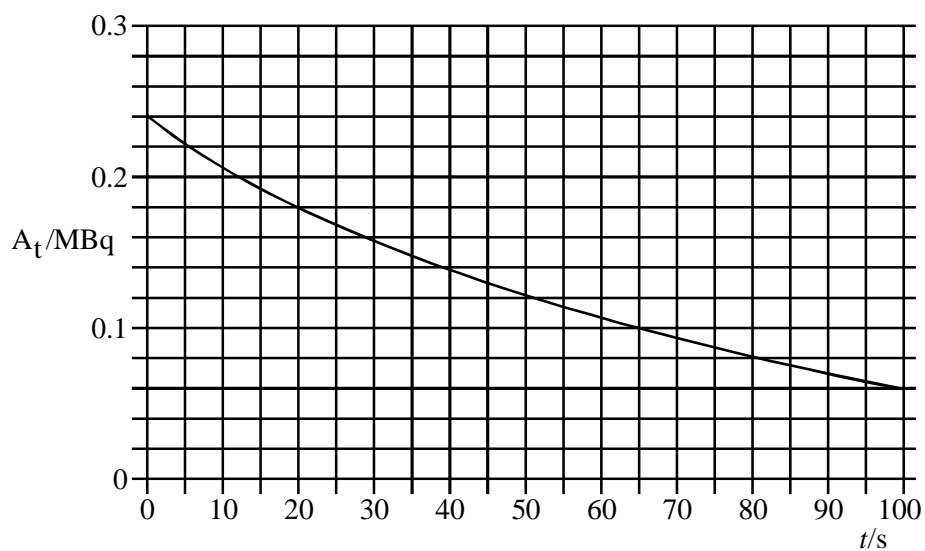
(b) Calculate the energy released, in MeV, in the fission reaction.

atomic mass of  $^{145}_{56}\text{Ba} = 144.92694\text{u}$

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(3)  
(Total 5 marks)

12. A radioactive nuclide decays by emitting  $\alpha$  particles. The graph shows how the rate of decay  $A$  of the source changes with time  $t$



(a) Determine

(i) the half-life of the nuclide,

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(ii) the decay constant,

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(iii) the initial number of undecayed nuclei present at time  $t = 0$ .

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(5)

(b) Each decay releases  $1.0 \times 10^{-12}$  J. For the time interval between  $t = 30$  s and  $t = 80$  s, calculate

(i) the number of nuclei which decay,

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(ii) the energy released.

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(4)

(Total 9 marks)

13. (a) In a nuclear reactor, energy is released as a result of *induced fission* of uranium  $-235$  nuclei.

(i) Explain what is meant by *induced fission*.

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(ii) Explain, using the charged liquid drop model, the energy changes in the fission of a

uranium -235 nucleus.

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(iii) Describe and explain how the fission of the uranium -235 nuclei in a fuel rod causes the fuel rods and the moderator to become very hot.

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(8)

- (b) When a uranium-235 nucleus undergoes fission, approximately 200 MeV of energy is released. Estimate the total mass of original fuel required per year in a 1600 MW nuclear reactor that uses enriched fuel containing 3% uranium-235 and 97% uranium-238 and operates at an efficiency of 25%.

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(5)  
(Total 13 marks)

14. (a) (i) Complete the equation below to represent the emission of an  $\alpha$  particle by a  ${}^{238}_{92}\text{U}$  isotope.



- (ii) Calculate the energy released when this  ${}^{238}_{92}\text{U}$  isotope nucleus emits an  $\alpha$  particle

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(5)

(b)  ${}_{92}^{238}\text{U}$  decays sequentially by emitting  $\alpha$  particles and  $\beta^-$  particles, eventually forming  ${}_{82}^{206}\text{Pb}$ , a stable isotope of lead.

(i) There are eight  $\alpha$  particles in the sequence.  
Calculate the number of  $\beta^-$  particles in the sequence.

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(ii) State the nuclear change that occurs during positron emission. Hence, explain why no positrons are emitted in this sequence.

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(6)  
(Total 11 marks)

15. A student attempted to determine the *half-life* of a radioactive substance, which emits  $\alpha$  particles, by placing it near a suitable counter. He recorded  $C$ , the number of counts in 30 s, at various times,  $t$ , after the start of the experiment.

The results given in the table were obtained.

t/minute	0	10	20	30	40	50	60
number of counts in 30s, $C$	60	42	35	23	18	14	10
$\ln C$							

(a) Explain what is meant by *half-life*.

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(1)

(b) Complete the table.

(1)

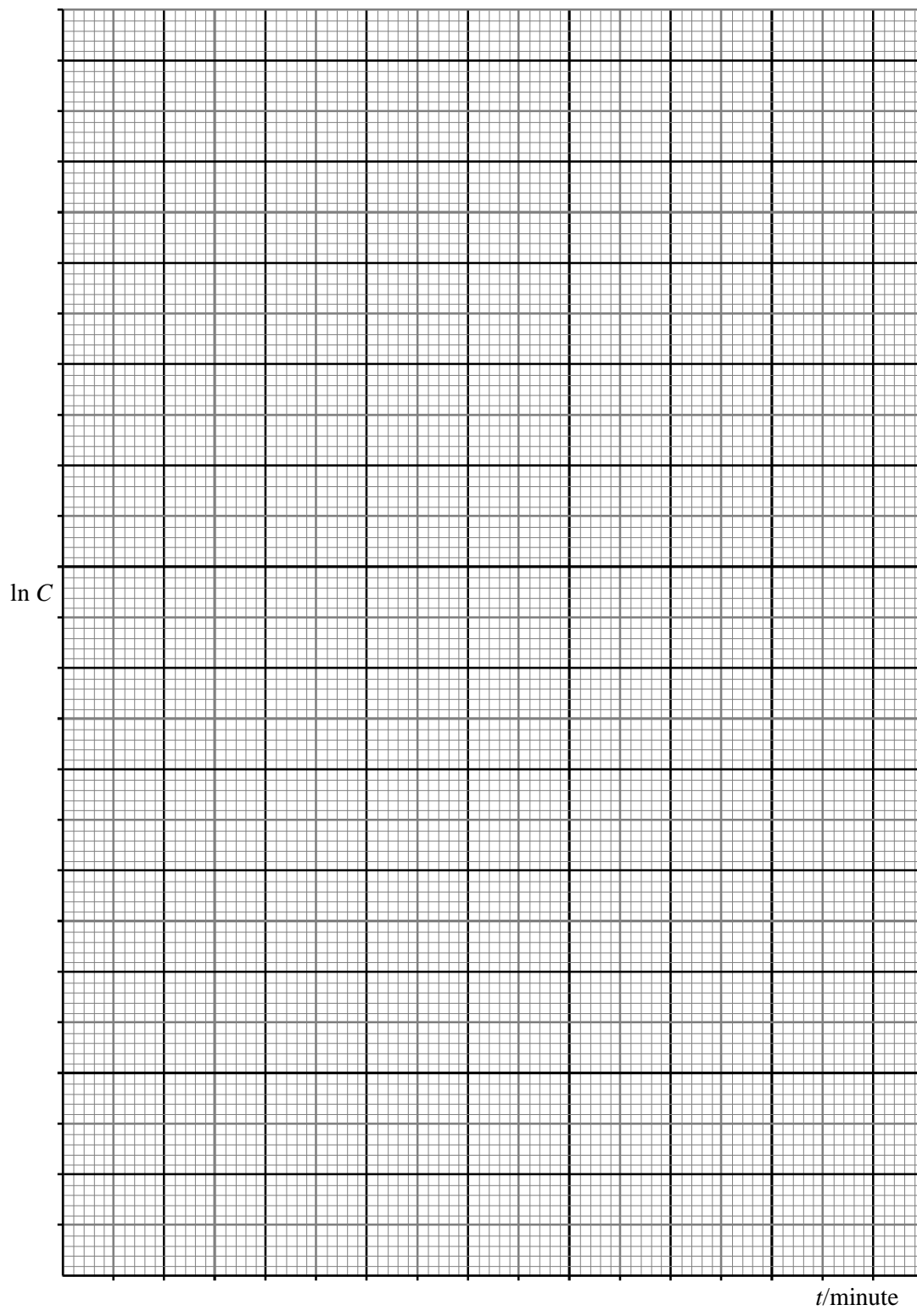
(c) On the grid below

(i) plot  $\ln C$  against  $t$ ,

(ii) draw the best straight line through your points,

(iii) determine the gradient of your graph.

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(5)

- (d) (i) Show that the decay constant of the substance is equal to the magnitude of the gradient of your graph.

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- (ii) Calculate the half-life of the substance.

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(3)

- (e) This particular experiment is likely to lead to an inaccurate value for the half-life. Suggest **two** ways in which the accuracy of the experiment could be improved.

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(2)



- (f) The age of a piece of bone recovered from an archaeological site may be estimated by  $^{14}\text{C}$  dating. All living organisms absorb  $^{14}\text{C}$  but there is no further intake after death. The proportion of  $^{14}\text{C}$  is constant in living organisms.

A 1 g sample of bone from an archaeological site has an average rate of decay of 5.2 Bq due to  $^{14}\text{C}$ . A 1 g sample of bone from a modern skeleton has a rate of decay of 6.5 Bq. The counts are corrected for background radiation.

Calculate the age, in years, of the archaeological samples of bone.

half life of  $^{14}\text{C} = 5730$  years

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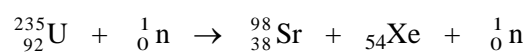
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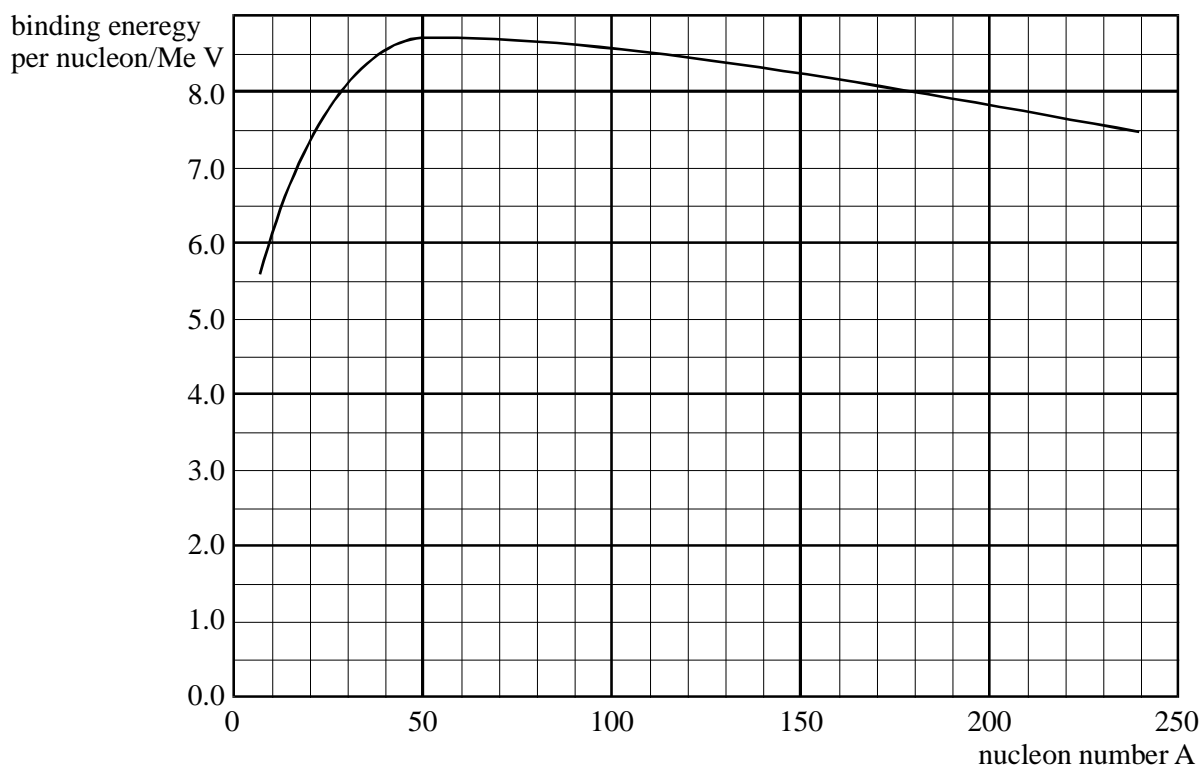
(4)  
(Total 16 marks)

16. (a) (i) Complete the equation below which represents the induced fission of a nucleus of uranium  $^{235}_{92}\text{U}$ .



- (ii) The graph shows the binding energy per nucleon plotted against nucleon number A.

Mark on the graph the position of each of the three nuclei in the equation.



- (iii) Hence determine the energy released in the fission process represented by the equation.

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(6)

- (b) (i) Use your answer to part (a)(iii) to estimate the energy released when 1.0 kg of uranium, containing 3% by mass of  ${}_{92}^{235}\text{U}$ , undergoes fission.

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- (ii) Oil releases approximately 50 MJ of heat per kg when it is burned in air. State and explain **one** advantage and **one** disadvantage of using nuclear fuel to produce electricity.

advantage .....

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disadvantage .....

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(6)  
(Total 12 marks)

17. (a) Show that the kinetic energy of an  $\alpha$  particle travelling at  $2.00 \times 10^7 \text{ ms}^{-1}$  is  $1.33 \times 10^{-12} \text{ J}$  when relativistic effects are ignored.

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(2)

- (b) Calculate the closest distance of approach for a head-on collision between the  $\alpha$  particle referred to in part (a) and a gold nucleus for which the proton number is 79. Assume that the gold nucleus remains stationary during the collision.

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(4)

- (c) State **one** reason why methods other than  $\alpha$  particle scattering are used to determine nuclear radii.

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(1)

(Total 7 marks)

18. Natural uranium consists of 99.3%  ${}_{92}^{238}\text{U}$  and 0.7%  ${}_{92}^{235}\text{U}$ . In many nuclear reactors, the fuel consists of enriched uranium enclosed in sealed metal containers.

- (a) (i) Explain what is meant by *enriched uranium*.

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- (ii) Why is enriched uranium rather than natural uranium used in many nuclear reactors?

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(2)

- (b) (i) By considering the neutrons involved in the fission process, explain how the rate of production of heat in a nuclear reactor is controlled.

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- (ii) Explain why all the fuel in a nuclear reactor is **not** placed in a single fuel rod.

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(5)

(Total 7 marks)

19. In an experiment to investigate the structure of the atom,  $\alpha$  particles were aimed at thin gold foil in a vacuum. A detector was used to determine the number of  $\alpha$  particles deflected through different angles.

- (a) State **two** observations about the  $\alpha$  particles detected coming from the foil.

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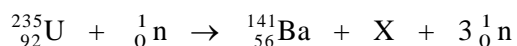
(2)

(b) State **two** features of the structure of the atom which can be deduced from these observations.

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(2)  
(Total 4 marks)

20. (a) Nuclear fission can occur when a neutron is absorbed by a nucleus of uranium-235. An incomplete equation for a typical fission reaction is given below.



(i) State the nuclear composition of X.

proton number .....

neutron number .....

(ii) Name the element of which X is an isotope.

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(3)

- (b) In a small nuclear power plant one fifth of the fission energy is converted into a useful output power of 10 MW. If the average energy released per fission is  $3.2 \times 10^{-11}$  J, calculate the number of uranium-235 nuclei which will undergo fission per day.

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(3)  
(Total 6 marks)